

# Contents

<i>Author biography</i>	xvii
<i>Preface</i>	xix
<b>1. Introduction</b>	<b>1</b>
1.1. Historical perspective	1
1.2. Fiber characteristics	3
1.2.1. Material and fabrication	4
1.2.2. Fiber losses	5
1.2.3. Chromatic dispersion	6
1.2.4. Polarization-mode dispersion	11
1.3. Fiber nonlinearities	15
1.3.1. Nonlinear refraction	15
1.3.2. Stimulated inelastic scattering	16
1.3.3. Importance of nonlinear effects	18
1.4. Overview	19
Problems	22
References	22
<b>2. Pulse propagation in fibers</b>	<b>27</b>
2.1. Maxwell's equations	27
2.2. Fiber modes	29
2.2.1. Eigenvalue equation	30
2.2.2. Characteristics of the fundamental mode	32
2.3. Pulse-propagation equation	34
2.3.1. Nonlinear wave equation	34
2.3.2. Higher-order nonlinear effects	40
2.3.3. Raman response function and its impact	42
2.4. Numerical methods	46
2.4.1. Split-step Fourier method	46
2.4.2. Finite-difference methods	50
Problems	52
References	53
<b>3. Group-velocity dispersion</b>	<b>57</b>
3.1. Different propagation regimes	57
3.2. Dispersion-induced pulse broadening	59
3.2.1. Gaussian pulses	60
3.2.2. Chirped Gaussian pulses	62
3.2.3. Hyperbolic secant pulses	64

3.2.4. Super-Gaussian pulses	65	5.2. Fiber solitons	138
3.2.5. Experimental results	68	5.2.1. Inverse scattering method	139
3.3. Third-order dispersion	69	5.2.2. Fundamental soliton	141
3.3.1. Chirped Gaussian pulses	70	5.2.3. Second and higher-order solitons	143
3.3.2. Broadening factor	71	5.2.4. Experimental confirmation	146
3.3.3. Ultrashort-pulse measurements	74	5.2.5. Soliton stability	147
3.4. Dispersion management	76	5.3. Other types of solitons	150
3.4.1. Dispersion compensation	76	5.3.1. Dark solitons	150
3.4.2. Compensation of third-order dispersion	78	5.3.2. Bistable solitons	154
3.4.3. Dispersion-varying fibers	80	5.3.3. Dispersion-managed solitons	155
Problems	81	5.3.4. Optical similaritons	156
References	82	5.4. Perturbation of solitons	159
<b>4. Self-phase modulation</b>	<b>85</b>	5.4.1. Perturbation methods	159
4.1. SPM-induced spectral changes	85	5.4.2. Fiber loss	160
4.1.1. Nonlinear phase shift	85	5.4.3. Soliton amplification	162
4.1.2. Changes in pulse spectra	88	5.4.4. Soliton interaction	165
4.1.3. Effect of pulse shape and initial chirp	90	5.5. Higher-order effects	169
4.1.4. Effect of partial coherence	93	5.5.1. Moment equations for pulse parameters	169
4.2. Effect of group-velocity dispersion	95	5.5.2. Third-order dispersion	171
4.2.1. Pulse evolution	96	5.5.3. Self-steepening	173
4.2.2. Broadening factor	98	5.5.4. Intrapulse Raman scattering	175
4.2.3. Optical wave breaking	100	5.6. Propagation of femtosecond pulses	180
4.2.4. Experimental results	103	Problems	182
4.2.5. Effect of third-order dispersion	104	References	183
4.2.6. SPM effects in fiber amplifiers	105		
4.3. Semianalytic techniques	108	<b>6. Polarization effects</b>	<b>189</b>
4.3.1. Moment method	108	6.1. Nonlinear birefringence	189
4.3.2. Variational method	110	6.1.1. Origin of nonlinear birefringence	190
4.3.3. Specific analytic solutions	111	6.1.2. Coupled-mode equations	192
4.4. Higher-order nonlinear effects	113	6.1.3. Elliptically birefringent fibers	193
4.4.1. Self-steepening	114	6.2. Nonlinear phase shift	194
4.4.2. Effect of GVD on optical shocks	117	6.2.1. Nondispersive XPM	194
4.4.3. Intrapulse Raman scattering	119	6.2.2. Optical Kerr effect	196
Problems	121	6.2.3. Pulse shaping	200
References	123	6.3. Evolution of polarization state	202
<b>5. Optical solitons</b>	<b>127</b>	6.3.1. Analytic solution	202
5.1. Modulation instability	127	6.3.2. Poincaré-sphere representation	204
5.1.1. Linear stability analysis	127	6.3.3. Polarization instability	207
5.1.2. Gain spectrum	129	6.3.4. Polarization chaos	210
5.1.3. Experimental observation	131	6.4. Vector modulation instability	210
5.1.4. Ultrashort pulse generation	132	6.4.1. Low-birefringence fibers	211
5.1.5. Impact of loss and third-order dispersion	134	6.4.2. High-birefringence fibers	213
5.1.6. Spatial modulation of fiber parameters	136	6.4.3. Isotropic fibers	215
		6.4.4. Experimental results	217

6.5. Birefringence and solitons	220	7.8. Two counterpropagating waves	288
6.5.1. Low-birefringence fibers	220	Problems	291
6.5.2. High-birefringence fibers	221	References	292
6.5.3. Soliton-dragging logic gates	225		
6.5.4. Vector solitons	226		
6.6. Higher-order effects	228	<b>8. Stimulated Raman scattering</b>	<b>297</b>
6.6.1. Extended coupled-mode equations	229	8.1. Basic concepts	297
6.6.2. Impact of TOD and Raman nonlinearity	230	8.1.1. Raman-gain spectrum	298
6.6.3. Interaction of two vector solitons	233	8.1.2. Raman threshold	299
6.7. Random birefringence	236	8.1.3. Coupled amplitude equations	302
6.7.1. Polarization-mode dispersion	236	8.1.4. Effect of four-wave mixing	305
6.7.2. Vector form of the NLS equation	237	8.2. Quasi-continuous SRS	307
6.7.3. Effects of PMD on solitons	239	8.2.1. Single-pass Raman generation	307
Problems	241	8.2.2. Raman fiber lasers	309
References	241	8.2.3. Raman fiber amplifiers	312
<b>7. Cross-phase modulation</b>	<b>245</b>	8.2.4. Raman-induced crosstalk	317
7.1. XPM-induced nonlinear coupling	245	8.3. SRS with short pump pulses	319
7.1.1. Nonlinear refractive index	245	8.3.1. Pulse-propagation equations	319
7.1.2. Coupled NLS equations	247	8.3.2. Nondispersive case	320
7.2. XPM-induced modulation instability	248	8.3.3. Effects of GVD	323
7.2.1. Linear stability analysis	248	8.3.4. Raman-induced index changes	326
7.2.2. Experimental results	250	8.3.5. Experimental results	327
7.3. XPM-paired solitons	252	8.3.6. Synchronously pumped Raman lasers	331
7.3.1. Bright-dark soliton pair	252	8.3.7. Short-pulse Raman amplification	332
7.3.2. Bright-gray soliton pair	253	8.4. Soliton effects	334
7.3.3. Periodic solutions	254	8.4.1. Raman solitons	334
7.3.4. Multiple coupled NLS equations	256	8.4.2. Raman soliton lasers	338
7.4. Spectral and temporal effects	257	8.4.3. Soliton-effect pulse compression	341
7.4.1. Asymmetric spectral broadening	258	8.5. Polarization effects	342
7.4.2. Asymmetric temporal changes	263	8.5.1. Vector theory of Raman amplification	342
7.4.3. Higher-order nonlinear effects	266	8.5.2. PMD effects on Raman amplification	346
7.5. Applications of XPM	267	Problems	349
7.5.1. XPM-induced pulse compression	267	References	350
7.5.2. XPM-induced optical switching	270		
7.5.3. XPM-induced wavelength conversion	271		
7.6. Polarization effects	272	<b>9. Stimulated Brillouin scattering</b>	<b>355</b>
7.6.1. Vector theory of XPM	272	9.1. Basic concepts	355
7.6.2. Polarization evolution	273	9.1.1. Physical process	355
7.6.3. Polarization-dependent spectral broadening	276	9.1.2. Brillouin-gain spectrum	356
7.6.4. Pulse trapping and compression	278	9.2. Quasi-CW SBS	360
7.6.5. XPM-induced wave breaking	281	9.2.1. Brillouin threshold	360
7.7. XPM effects in birefringent fibers	282	9.2.2. Polarization effects	361
7.7.1. Fibers with low birefringence	283	9.2.3. Techniques for controlling the SBS threshold	363
7.7.2. Fibers with high birefringence	287	9.2.4. Experimental results	365

<b>9.4. SBS dynamics</b>	372	<b>11. Highly nonlinear fibers</b>	<b>463</b>
9.4.1. Coupled amplitude equations	372	11.1. Nonlinear parameter	463
9.4.2. SBS with Q-switched pulses	374	11.1.1. Units and values of $n_2$	463
9.4.3. SBS-induced index changes	378	11.1.2. SPM-based techniques	465
9.4.4. Relaxation oscillations	383	11.1.3. XPM-based technique	468
9.4.5. Modulation instability and chaos	385	11.1.4. FWM-based technique	469
<b>9.5. Brillouin fiber lasers</b>	387	11.1.5. Variations in $n_2$ values	471
9.5.1. CW operation	387	11.2. Fibers with silica cladding	474
9.5.2. Pulsed operation	391	11.3. Tapered fibers with air cladding	476
Problems	394	11.4. Microstructured fibers	480
References	395	11.4.1. Design and fabrication	480
		11.4.2. Modal and dispersive properties	482
		11.4.3. Hollow-core photonic crystal fibers	485
<b>10. Four-wave mixing</b>	<b>401</b>	11.4.4. Bragg fibers	486
10.1. Origin of four-wave mixing	401	11.5. Non-silica fibers	487
10.2. Theory of four-wave mixing	403	11.5.1. Lead-silicate fibers	488
10.2.1. Coupled amplitude equations	404	11.5.2. Chalcogenide fibers	491
10.2.2. Approximate solution	405	11.5.3. Bismuth-oxide fibers	492
10.2.3. Effect of phase matching	406	11.6. Theory of narrow-core fibers	493
10.2.4. Ultrafast four-wave mixing	408	Problems	498
<b>10.3. Phase-matching techniques</b>	409	References	499
10.3.1. Physical mechanisms	410		
10.3.2. Nearly phase-matched four-wave mixing	411		
10.3.3. Phase matching near the zero-dispersion wavelength	412	<b>12. Novel nonlinear phenomena</b>	<b>503</b>
10.3.4. Phase matching through self-phase modulation	413	12.1. Soliton fission and dispersive waves	503
10.3.5. Phase matching in birefringent fibers	416	12.1.1. Fission of second- and higher-order solitons	503
<b>10.4. Parametric amplification</b>	419	12.1.2. Generation of dispersive waves	507
10.4.1. Review of early work	419	12.2. Intrapulse Raman scattering	512
10.4.2. Gain spectrum and its bandwidth	421	12.2.1. Enhanced RIFS through soliton fission	512
10.4.3. Single-pump configuration	423	12.2.2. Cross-correlation technique	516
10.4.4. Dual-pump configuration	427	12.2.3. Wavelength tuning through RIFS	518
10.4.5. Effects of pump depletion	432	12.2.4. Effects of birefringence	521
<b>10.5. Polarization effects</b>	434	12.2.5. Suppression of Raman-induced frequency shifts	523
10.5.1. Vector theory of four-wave mixing	435	12.2.6. Soliton dynamics near a zero-dispersion wavelength	527
10.5.2. Polarization dependence of parametric gain	437	12.2.7. Multipeak Raman solitons	530
10.5.3. Linearly and circularly polarized pumps	440	12.3. Frequency combs and cavity solitons	532
10.5.4. Effect of residual fiber birefringence	443	12.3.1. CW-pumped ring cavities	533
<b>10.6. Applications of four-wave mixing</b>	446	12.3.2. Nonlinear dynamics of ring cavities	534
10.6.1. Parametric amplifiers and wavelength converters	446	12.3.3. Frequency combs without a cavity	537
10.6.2. Tunable fiber-optic parametric oscillators	448	12.4. Second-harmonic generation	538
10.6.3. Ultrafast signal processing	451	12.4.1. Physical mechanisms	539
10.6.4. Quantum correlation and noise squeezing	453	12.4.2. Thermal poling and quasi-phase matching	541
10.6.5. Phase-sensitive amplification	456	12.4.3. SHG theory	544
Problems	457	12.5. Third-harmonic generation	546
References	458	12.5.1. THG in highly nonlinear fibers	546
		12.5.2. Effects of group-velocity mismatch	547

12.5.3. Effects of fiber birefringence	549	14.3.2. Multimode solitons	644
Problems	551	14.3.3. Solitons in specific fiber modes	649
References	552	14.4. Intermodal nonlinear phenomena	651
<b>13. Supercontinuum generation</b>	<b>557</b>	14.4.1. Intermodal FWM	651
13.1. Pumping with picosecond pulses	557	14.4.2. Intermodal SRS	657
13.1.1. Nonlinear mechanisms	558	14.4.3. Intermodal SBS	662
13.1.2. Experimental progress after 2000	560	14.5. Spatio-temporal dynamics	665
13.2. Pumping with femtosecond pulses	563	14.5.1. Spatial beam cleanup	666
13.3. Temporal and spectral evolution of pulses	568	14.5.2. Supercontinuum generation	668
13.3.1. Numerical modeling of supercontinuum	569	14.6. Multicore fibers	674
13.3.2. Role of cross-phase modulation	572	Problems	678
13.3.3. XPM-induced trapping	575	References	679
13.3.4. Role of four-wave mixing	580	<b>A. System of units</b>	685
13.4. CW or quasi-CW pumping	581	<b>B. Nonlinear response of fibers</b>	687
13.4.1. Nonlinear mechanisms	582	References	688
13.4.2. Experimental results	585	<b>C. Derivation of the generalized NLS equation</b>	689
13.5. Polarization effects	588	<b>D. Numerical code for the NLS equation</b>	693
13.6. Coherence properties	593	<b>E. List of acronyms</b>	695
13.6.1. Effect of pump coherence	593	<i>Index</i>	697
13.6.2. Spectral incoherent solitons	596		
13.6.3. Techniques for improving spectral coherence	599		
13.7. Ultraviolet and mid-infrared supercontinua	601		
13.7.1. Extension into ultraviolet region	602		
13.7.2. Extension into mid-infrared region	604		
13.8. Optical rogue waves	607		
13.8.1. L-shaped statistics of pulse-to-pulse fluctuations	607		
13.8.2. Techniques for controlling rogue-wave statistics	608		
13.8.3. Modulation instability revisited	611		
Problems	614		
References	615		
<b>14. Multimode fibers</b>	<b>621</b>		
14.1. Modes of optical fibers	621		
14.1.1. Step-index fibers	621		
14.1.2. Graded-index fibers	625		
14.1.3. Multicore fibers	627		
14.1.4. Excitation of fiber modes	630		
14.2. Nonlinear pulse propagation	631		
14.2.1. Multimode propagation equations	631		
14.2.2. Few-mode fibers	633		
14.2.3. Random linear mode coupling	635		
14.2.4. Graded-index fibers	638		
14.3. Modulation instability and solitons	640		
14.3.1. Modulation instability	641		