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*Web: The Supplemental Chapters 8 and 9 can be downloaded from the web page: (www.prenhall.com/Leon)
†Optional sections.