Contents

Preface xi To the Student xvii Suggested Lecture Schedule xix

1 The Geometry of the Plane and 3-Space 1

- **1.1** Vectors 1
- **1.2** Length and Direction 16
- 1.3 Lines, Planes, and the Cross Product of Vectors 26
- 1.4 Projections 45
- **1.5** Euclidean *n*-Space 54 Review Exercises 66

2 Matrices and Linear Equations 69

- 2.1 The Algebra of Matrices 69
- 2.2 The Inverse and Transpose of a Matrix 88
- 2.3 Systems of Linear Equations 98
- 2.4 Homogeneous Systems and Linear Independence 117
- 2.5 The LU Factorization of a Matrix 125
- 2.6 LDU Factorizations 144
- 2.7 Finding the Inverse of a Matrix 152 Review Exercises 163

3 Determinants, Eigenvalues, Eigenvectors 167

- 3.1 The Determinant of a Matrix 167
- 3.2 Properties of Determinants 177
- 3.3 The Eigenvalues and Eigenvectors of a Matrix 193
- **3.4** Similarity and Diagonalization 203 Review Exercises 214

4 Vector Spaces 217

- 4.1 The Theory of Linear Equations 217
- **4.2** Basic Terminology and Concepts 233
- 4.3 Basis and Dimension; Rank and Nullity 253
- 4.4 One-Sided Inverses 274 Review Exercises 282

5 Linear Transformations 285

- **5.1** Linear Transformations of R^n 285
- 5.2 Matrix Multiplication Revisited 301
- 5.3 The Matrices of a Linear Transformation 308
- 5.4 Changing Coordinates 321 Review Exercises 331

6 Orthogonality 335

- 6.1 Projection Matrices and Least Squares Approximation 335
- 6.2 The Gram–Schmidt Algorithm and QR Factorization 353
- 6.3 Orthogonal Subspaces and Complements 371
- 6.4 The Pseudoinverse of a Matrix 387 Review Exercises 398

7 The Spectral Theorem 401

- 7.1 Complex Numbers and Vectors 401
- 7.2 Complex Matrices 415
- 7.3 Unitary Diagonalization 423
- 7.4 Real Symmetric Matrices 441
- 7.5 The Singular Value Decomposition 448 Review Exercises 455

8 Applications 457

- 8.1 Data Fitting 457
- 8.2 Linear Recurrence Relations 462
- 8.3 Markov Processes 468
- 8.4 Quadratic Forms and Conic Sections 474
- 8.5 Graphs 479

Appendix: Show and Prove A-1

Solutions to True/False Questions and Selected Exercises *S-1*

Glossary G-1

Index *I-1*