

Preface to the First Edition xix

Preface to the Fourth Edition xxiii

PART 1 **Fundamental Principles 1**

Chapter 1

Aerodynamics: Some Introductory Thoughts 3

- 1.1** Importance of Aerodynamics: Historical Examples 5
- 1.2** Aerodynamics: Classification and Practical Objectives 11
- 1.3** Road Map for This Chapter 14
- 1.4** Some Fundamental Aerodynamic Variables 15
 - 1.4.1 Units 18*
- 1.5** Aerodynamic Forces and Moments 19
- 1.6** Center of Pressure 32
- 1.7** Dimensional Analysis: The Buckingham Pi Theorem 34
- 1.8** Flow Similarity 40
- 1.9** Fluid Statics: Buoyancy Force 51
- 1.10** Types of Flow 57
 - 1.10.1 Continuum Versus Free Molecule Flow 58*
 - 1.10.2 Inviscid Versus Viscous Flow 58*
 - 1.10.3 Incompressible Versus Compressible Flows 60*
 - 1.10.4 Mach Number Regimes 60*
- 1.11** Viscous Flow: Introduction to Boundary Layers 64

1.12 Applied Aerodynamics: The Aerodynamic Coefficients—Their Magnitudes and Variations 71

1.13 Historical Note: The Illusive Center of Pressure 83

1.14 Historical Note: Aerodynamic Coefficients 87

1.15 Summary 91

1.16 Problems 92

Chapter 2

Aerodynamics: Some Fundamental Principles and Equations 95

- 2.1** Introduction and Road Map 96
- 2.2** Review of Vector Relations 97
 - 2.2.1 Some Vector Algebra 98*
 - 2.2.2 Typical Orthogonal Coordinate Systems 99*
 - 2.2.3 Scalar and Vector Fields 102*
 - 2.2.4 Scalar and Vector Products 102*
 - 2.2.5 Gradient of a Scalar Field 103*
 - 2.2.6 Divergence of a Vector Field 105*
 - 2.2.7 Curl of a Vector Field 106*
 - 2.2.8 Line Integrals 106*
 - 2.2.9 Surface Integrals 107*
 - 2.2.10 Volume Integrals 108*
 - 2.2.11 Relations Between Line, Surface, and Volume Integrals 109*
 - 2.2.12 Summary 109*
- 2.3** Models of the Fluid: Control Volumes and Fluid Elements 109
 - 2.3.1 Finite Control Volume Approach 110*
 - 2.3.2 Infinitesimal Fluid Element Approach 111*
 - 2.3.3 Molecular Approach 111*

| | | | | | |
|--|---|-----|-------|--|-----|
| 2.3.4 | <i>Physical Meaning of the Divergence of Velocity</i> | 112 | 3.3 | Incompressible Flow in a Duct: The Venturi and Low-Speed Wind Tunnel | 197 |
| 2.3.5 | <i>Specification of the Flow Field</i> | 113 | 3.4 | Pitot Tube: Measurement of Airspeed | 210 |
| 2.4 | Continuity Equation | 117 | 3.5 | Pressure Coefficient | 219 |
| 2.5 | Momentum Equation | 122 | 3.6 | Condition on Velocity for Incompressible Flow | 221 |
| 2.6 | An Application of the Momentum Equation: Drag of a Two-Dimensional Body | 127 | 3.7 | Governing Equation for Irrotational, Incompressible Flow: Laplace's Equation | 222 |
| 2.6.1 | <i>Comment</i> | 136 | 3.7.1 | <i>Infinity Boundary Conditions</i> | 225 |
| 2.7 | Energy Equation | 136 | 3.7.2 | <i>Wall Boundary Conditions</i> | 225 |
| 2.8 | Interim Summary | 141 | 3.8 | Interim Summary | 226 |
| 2.9 | Substantial Derivative | 142 | 3.9 | Uniform Flow: Our First Elementary Flow | 227 |
| 2.10 | Fundamental Equations in Terms of the Substantial Derivative | 145 | 3.10 | Source Flow: Our Second Elementary Flow | 229 |
| 2.11 | Pathlines, Streamlines, and Streaklines of a Flow | 147 | 3.11 | Combination of a Uniform Flow with a Source and Sink | 233 |
| 2.12 | Angular Velocity, Vorticity, and Strain | 152 | 3.12 | Doublet Flow: Our Third Elementary Flow | 237 |
| 2.13 | Circulation | 162 | 3.13 | Nonlifting Flow over a Circular Cylinder | 239 |
| 2.14 | Stream Function | 165 | 3.14 | Vortex Flow: Our Fourth Elementary Flow | 245 |
| 2.15 | Velocity Potential | 169 | 3.15 | Lifting Flow over a Cylinder | 249 |
| 2.16 | Relationship Between the Stream Function and Velocity Potential | 171 | 3.16 | The Kutta-Joukowski Theorem and the Generation of Lift | 262 |
| 2.17 | How Do We Solve the Equations? | 172 | 3.17 | Nonlifting Flows over Arbitrary Bodies: The Numerical Source Panel Method | 264 |
| 2.17.1 | <i>Theoretical (Analytical) Solutions</i> | 172 | 3.18 | Applied Aerodynamics: The Flow over a Circular Cylinder—The Real Case | 274 |
| 2.17.2 | <i>Numerical Solutions—Computational Fluid Dynamics (CFD)</i> | 174 | 3.19 | Historical Note: Bernoulli and Euler—The Origins of Theoretical Fluid Dynamics | 282 |
| 2.17.3 | <i>The Bigger Picture</i> | 181 | 3.20 | Historical Note: d'Alembert and His Paradox | 287 |
| 2.18 | Summary | 181 | 3.21 | Summary | 288 |
| 2.19 | Problems | 185 | 3.22 | Problems | 291 |
| | | | | | |
| PART 2 | | | | | |
| Inviscid, Incompressible Flow 187 | | | | | |
| | | | | | |
| Chapter 3 | | | | | |
| Fundamentals of Inviscid, Incompressible Flow 189 | | | | | |
| 3.1 | Introduction and Road Map | 190 | | | |
| 3.2 | Bernoulli's Equation | 193 | | | |

| | |
|--|---|
| Chapter 4 | Chapter 5 |
| Incompressible Flow over Airfoils 295 | Incompressible Flow over Finite Wings 391 |
| 1 Introduction 297 | 5.1 Introduction: Downwash and Induced Drag 395 |
| 2 Airfoil Nomenclature 300 | 5.2 The Vortex Filament, the Biot-Savart Law, and Helmholtz's Theorems 400 |
| 3 Airfoil Characteristics 302 | 5.3 Prandtl's Classical Lifting-Line Theory 404 |
| 4 Philosophy of Theoretical Solutions for Low-Speed Flow over Airfoils: The Vortex Sheet 307 | 5.3.1 <i>Elliptical Lift Distribution</i> 410 |
| 5 The Kutta Condition 312 | 5.3.2 <i>General Lift Distribution</i> 415 |
| 4.5.1 <i>Without Friction Could We Have Lift?</i> 316 | 5.3.3 <i>Effect of Aspect Ratio</i> 418 |
| 6 Kelvin's Circulation Theorem and the Starting Vortex 316 | 5.3.4 <i>Physical Significance</i> 424 |
| 7 Classical Thin Airfoil Theory: The Symmetric Airfoil 319 | 5.4 A Numerical Nonlinear Lifting-Line Method 433 |
| 8 The Cambered Airfoil 329 | 5.5 The Lifting-Surface Theory and the Vortex Lattice Numerical Method 437 |
| 9 The Aerodynamic Center: Additional Considerations 338 | 5.6 Applied Aerodynamics: The Delta Wing 444 |
| 10 Lifting Flows over Arbitrary Bodies: The Vortex Panel Numerical Method 342 | 5.7 Historical Note: Lanchester and Prandtl—The Early Development of Finite-Wing Theory 456 |
| 11 Modern Low-Speed Airfoils 348 | 5.8 Historical Note: Prandtl—The Man 460 |
| 12 Viscous Flow: Airfoil Drag 352 | 5.9 Summary 463 |
| 4.12.1 <i>Estimating Skin-Friction Drag: Laminar Flow</i> 353 | 5.10 Problems 464 |
| 4.12.2 <i>Estimating Skin-Friction Drag: Turbulent Flow</i> 355 | |
| 4.12.3 <i>Transition</i> 357 | Chapter 6 |
| 4.12.4 <i>Flow Separation</i> 362 | Three-Dimensional Incompressible Flow 467 |
| 4.12.5 <i>Comment</i> 367 | 6.1 Introduction 467 |
| 13 Applied Aerodynamics: The Flow over an Airfoil—The Real Case 368 | 6.2 Three-Dimensional Source 468 |
| 14 Historical Note: Early Airplane Design and the Role of Airfoil Thickness 379 | 6.3 Three-Dimensional Doublet 470 |
| 15 Historical Note: Kutta, Joukowski, and the Circulation Theory of Lift 384 | 6.4 Flow over a Sphere 472 |
| 16 Summary 386 | 6.4.1 <i>Comment on the Three-Dimensional Relieving Effect</i> 474 |
| 17 Problems 388 | 6.5 General Three-Dimensional Flows: Panel Techniques 475 |
| | 6.6 Applied Aerodynamics: The Flow over a Sphere—The Real Case 477 |
| | 6.7 Summary 480 |
| | 6.8 Problems 481 |

CONTENTS

PART 3
Inviscid, Compressible Flow 483

Chapter 7

Compressible Flow: Some Preliminary Aspects 485

- 7.1** Introduction 486
- 7.2** A Brief Review of Thermodynamics 488
 - 7.2.1 *Perfect Gas* 488
 - 7.2.2 *Internal Energy and Enthalpy* 488
 - 7.2.3 *First Law of Thermodynamics* 492
 - 7.2.4 *Entropy and the Second Law of Thermodynamics* 493
 - 7.2.5 *Iisentropic Relations* 495
- 7.3** Definition of Compressibility 497
- 7.4** Governing Equations for Inviscid, Compressible Flow 499
- 7.5** Definition of Total (Stagnation) Conditions 501
- 7.6** Some Aspects of Supersonic Flow: Shock Waves 507
- 7.7** Summary 510
- 7.8** Problems 513

Chapter 8

Normal Shock Waves and Related Topics 515

- 8.1** Introduction 516
- 8.2** The Basic Normal Shock Equations 517
- 8.3** Speed of Sound 521
- 8.4** Special Forms of the Energy Equation 527
- 8.5** When Is a Flow Compressible? 534
- 8.6** Calculation of Normal Shock-Wave Properties 537
- 8.7** Measurement of Velocity in a Compressible Flow 548
 - 8.7.1 *Subsonic Compressible Flow* 548
 - 8.7.2 *Supersonic Flow* 549

8.8 Summary 553

8.9 Problems 556

Chapter 9

Oblique Shock and Expansion Waves 559

- 9.1** Introduction 560
- 9.2** Oblique Shock Relations 566
- 9.3** Supersonic Flow over Wedges and Cones 580
- 9.4** Shock Interactions and Reflections 583
- 9.5** Detached Shock Wave in Front of a Blunt Body 589
- 9.6** Prandtl-Meyer Expansion Waves 591
- 9.7** Shock-Expansion Theory: Applications to Supersonic Airfoils 602
- 9.8** A Comment on Lift and Drag Coefficients 606
- 9.9** Viscous Flow: Shock-Wave/Boundary-Layer Interaction 606
- 9.10** Historical Note: Ernst Mach—A Biographical Sketch 609
- 9.11** Summary 611
- 9.12** Problems 612

Chapter 10

Compressible Flow Through Nozzles, Diffusers, and Wind Tunnels 617

- 10.1** Introduction 618
- 10.2** Governing Equations for Quasi-One-Dimensional Flow 620
- 10.3** Nozzle Flows 629
 - 10.3.1 *More on Mass Flow* 643
- 10.4** Diffusers 644
- 10.5** Supersonic Wind Tunnels 646
- 10.6** Viscous Flow: Shock-Wave/Boundary-Layer Interaction Inside Nozzles 652
- 10.7** Summary 654
- 10.8** Problems 655

Chapter 11**Subsonic Compressible Flow over Airfoils:
Linear Theory 657**

- 11.1** Introduction 658
- 11.2** The Velocity Potential Equation 660
- 11.3** The Linearized Velocity Potential Equation 663
- 11.4** Prandtl-Glauert Compressibility Correction 668
- 11.5** Improved Compressibility Corrections 673
- 11.6** Critical Mach Number 674
 - 11.6.1 A Comment on the Location of Minimum Pressure (Maximum Velocity) 683*
- 11.7** Drag-Divergence Mach Number: The Sound Barrier 683
- 11.8** The Area Rule 691
- 11.9** The Supercritical Airfoil 693
- 11.10** CFD Applications: Transonic Airfoils and Wings 695
- 11.11** Historical Note: High-Speed Airfoils—Early Research and Development 700
- 11.12** Historical Note: Richard T. Whitcomb—Architect of the Area Rule and the Supercritical Wing 704
- 11.13** Summary 706
- 11.14** Problems 707

Chapter 12**Linearized Supersonic Flow 709**

- 12.1** Introduction 710
- 12.2** Derivation of the Linearized Supersonic Pressure Coefficient Formula 710
- 12.3** Application to Supersonic Airfoils 714
- 12.4** Viscous Flow: Supersonic Airfoil Drag 720
- 12.5** Summary 723
- 12.6** Problems 724

Chapter 13**Introduction to Numerical Techniques
for Nonlinear Supersonic Flow 725**

- 13.1** Introduction: Philosophy of Computational Fluid Dynamics 726
- 13.2** Elements of the Method of Characteristics 728
 - 13.2.1 Internal Points 734*
 - 13.2.2 Wall Points 735*
- 13.3** Supersonic Nozzle Design 736
- 13.4** Elements of Finite-Difference Methods 739
 - 13.4.1 Predictor Step 745*
 - 13.4.2 Corrector Step 745*
- 13.5** The Time-Dependent Technique: Application to Supersonic Blunt Bodies 746
 - 13.5.1 Predictor Step 750*
 - 13.5.2 Corrector Step 750*
- 13.6** Summary 754
- 13.7** Problem 754

Chapter 14**Elements of Hypersonic Flow 757**

- 14.1** Introduction 758
- 14.2** Qualitative Aspects of Hypersonic Flow 759
- 14.3** Newtonian Theory 763
- 14.4** The Lift and Drag of Wings at Hypersonic Speeds: Newtonian Results for a Flat Plate at Angle of Attack 767
 - 14.4.1 Accuracy Considerations 774*
- 14.5** Hypersonic Shock-Wave Relations and Another Look at Newtonian Theory 778
- 14.6** Mach Number Independence 782
- 14.7** Hypersonics and Computational Fluid Dynamics 784
- 14.8** Summary 787
- 14.9** Problems 787

PART 4

Viscous Flow 789

Chapter 15

Introduction to the Fundamental Principles and Equations of Viscous Flow 791

- 15.1 Introduction 792
- 15.2 Qualitative Aspects of Viscous Flow 793
- 15.3 Viscosity and Thermal Conduction 801
- 15.4 The Navier-Stokes Equations 806
- 15.5 The Viscous Flow Energy Equation 810
- 15.6 Similarity Parameters 814
- 15.7 Solutions of Viscous Flows: A Preliminary Discussion 818
- 15.8 Summary 821
- 15.9 Problems 823

Chapter 16

Some Special Cases; Couette and Poiseuille Flows 825

- 16.1 Introduction 825
- 16.2 Couette Flow: General Discussion 826
- 16.3 Incompressible (Constant Property) Couette Flow 830
 - 16.3.1 Negligible Viscous Dissipation 836
 - 16.3.2 Equal Wall Temperatures 837
 - 16.3.3 Adiabatic Wall Conditions (Adiabatic Wall Temperature) 839
 - 16.3.4 Recovery Factor 842
 - 16.3.5 Reynolds Analogy 843
 - 16.3.6 Interim Summary 844
- 16.4 Compressible Couette Flow 846
 - 16.4.1 Shooting Method 848
 - 16.4.2 Time-Dependent Finite-Difference Method 850
 - 16.4.3 Results for Compressible Couette Flow 854
 - 16.4.4 Some Analytical Considerations 856

16.5 Two-Dimensional Poiseuille Flow 861

16.6 Summary 865

16.6.1 Couette Flow 865

16.6.2 Poiseuille Flow 865

Chapter 17

Introduction to Boundary Layers 867

- 17.1 Introduction 868
- 17.2 Boundary-Layer Properties 870
- 17.3 The Boundary-Layer Equations 876
- 17.4 How Do We Solve the Boundary-Layer Equations? 879
- 17.5 Summary 881

Chapter 18

Laminar Boundary Layers 883

- 18.1 Introduction 883
- 18.2 Incompressible Flow over a Flat Plate: The Blasius Solution 884
- 18.3 Compressible Flow over a Flat Plate 891
 - 18.3.1 A Comment on Drag Variation with Velocity 902
- 18.4 The Reference Temperature Method 903
 - 18.4.1 Recent Advances: The Meador-Smart Reference Temperature Method 906
- 18.5 Stagnation Point Aerodynamic Heating 907
- 18.6 Boundary Layers over Arbitrary Bodies: Finite-Difference Solution 913
 - 18.6.1 Finite-Difference Method 914
- 18.7 Summary 919
- 18.8 Problems 920

Chapter 19

Turbulent Boundary Layers 921

- 19.1 Introduction 922
- 19.2 Results for Turbulent Boundary Layers on a Flat Plate 922

| | | |
|---|---|-----|
| 19.2.1 | <i>Reference Temperature Method for Turbulent Flow</i> | 924 |
| 19.2.2 | <i>The Meador-Smart Reference Temperature Method for Turbulent Flow</i> | 926 |
| 19.2.3 | <i>Prediction of Airfoil Drag</i> | 927 |
| 19.3 | Turbulence Modeling | 927 |
| 19.3.1 | <i>The Baldwin-Lomax Model</i> | 928 |
| 19.4 | Final Comments | 930 |
| 19.5 | Summary | 931 |
| 19.6 | Problems | 932 |
| | | |
| Chapter 20 | | |
| Navier-Stokes Solutions: Some Examples 933 | | |
| 20.1 | Introduction | 934 |
| 20.2 | The Approach | 934 |
| 20.3 | Examples of Some Solutions | 935 |
| 20.3.1 | <i>Flow over a Rearward-Facing Step</i> | 935 |
| 20.3.2 | <i>Flow over an Airfoil</i> | 935 |
| 20.3.3 | <i>Flow over a Complete Airplane</i> | 938 |
| 20.3.4 | <i>Shock-Wave/Boundary-Layer Interaction</i> | 939 |
| 20.3.5 | <i>Flow over an Airfoil with a Protuberance</i> | 940 |

| | | |
|------|--|-----|
| 20.4 | The Issue of Accuracy for the Prediction of Skin Friction Drag | 942 |
|------|--|-----|

| | | |
|------|---------|-----|
| 20.5 | Summary | 947 |
|------|---------|-----|

| | | |
|-------------------|-----------------------------------|------------|
| Appendix A | Isentropic Flow Properties | 949 |
|-------------------|-----------------------------------|------------|

| | | |
|-------------------|--------------------------------|------------|
| Appendix B | Normal Shock Properties | 955 |
|-------------------|--------------------------------|------------|

| | | |
|-------------------|--|------------|
| Appendix C | Prandtl-Meyer Function and Mach Angle | 959 |
|-------------------|--|------------|

| | | |
|-------------------|--------------------------------------|------------|
| Appendix D | Standard Atmosphere, SI Units | 963 |
|-------------------|--------------------------------------|------------|

| | | |
|-------------------|---|------------|
| Appendix E | Standard Atmosphere, English Engineering Units | 973 |
|-------------------|---|------------|

| | |
|---------------------|------------|
| Bibliography | 981 |
|---------------------|------------|

| | |
|--------------|------------|
| Index | 987 |
|--------------|------------|